

## Dynamic Analysis of Wheel-Rail Interaction Stress Distribution for ENR Locomotives

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### ABSTRACT

Egyptian rails have gotten worn as a result of a lack of upkeep and inadequate rail grinding. If the new locomotives are designed to work with standard tracks, they should be able to move more efficiently and safely on standard rails than worn ones that were not designed for standard tracks. The contact stress variation brought on by variations in the wheel-rail contact profile has a significant impact on the safety of railway traffic. In this article, a standard rail UIC54 and a wheel profile as per Egyptian Railway standards are taken into consideration to explore the impact of interacting wheel and rail profile topology. Standard rail and a real worn rail from the Egyptian National Railways (ENR) have different rail profile radii. The problem is undertaken using ANSYS Finite Element Method (FEM). All required elements of the rail system were modeled for analyses., such as rail, wheel, and axle. These tools obtain the distribution of contact stress, contact pressure, and fatigue for standard and damaged rail profiles. Using stress distribution obtained through FEM analysis, the effects of the change in Egyptian rail profiles with ENR New locomotives' wheel on the contact stress is investigated. Contact stresses for the worn rail profile are up to 40% lower than those for an unused ENR rail profile. As the worn rail has a larger contact area than the standard rail, there is a reduction in the life cycles to failure., and fatigue damage rises as the contact stresses decrease.

Keywords: Wheel-rail contact stresses, Finite Element Analysis, wear, ANSYS

## 1 INTRODUCTION

Rail defects are a common problem in Egypt's railway system, which can pose serious risks to passenger safety and cause disruptions to the country's transportation network. Any imperfection or damage to the rail infrastructure that might compromise its overall strength, durability, or performance is referred to as a track problem.

Examples of common types of rail defects in Egypt include worn rails, defective joints or welds, and broken or missing fasteners such as clips, bolts, and screws. These defects can occur due to various reasons such as heavy or insufficient investment in the railway system.

Egyptian rails have gotten worn due to a lack of upkeep and inadequate rail grinding. If the new locomotives are designed to work with standard tracks, they should be able to move more efficiently and safely on standard rails than worn ones not designed for standard tracks.

All studies on how vehicles and tracks interact are built around a wheel's contact with a rail. Through the process of the stresses it transmits, this small interface controls the dynamic performance of locomotives. It is vulnerable to severe damaging occurrences, much like any area of high stress. To accurately simulate vehicle dynamics and conduct damage studies, it is crucial to understand the mechanism of contact through wheel and rail. The Hertz technique has been used extensively in research on contact interaction in a pair of wheel rails[1]. The Hertz hypothesis has served as the foundation for several analytical techniques that have been developed to study the contact between moving wheel-rail surfaces. Several scholars have developed a way to determine the equation of Hertz for contact area, penetration, and contact pressure. [2]. By getting close to the elliptic axis ratio, the researchers have tried to numerically simplify the solution to the elliptic integral. Tanaka developed a new technique for calculating elliptical Hertz contact pressure that does not need the calculation of an elliptic integral[3]. polynomial estimation was used in place of the elliptical integral to generate a hypothetical Hertzian contact model[4]. The elliptical integral was simplified by the researchers using an innovative method, and the outcome exhibits good agreement with the theoretical findings. In addition to employing analytical-numerical approximation, FEM was used in the year 2000 to solve the Hertzian contact issue related to wheel-rail contact[5]. Three different approaches, namely the Hertz theory, FEM, and software contact from Kalker, have been used to compare the contact pressure calculations. Next, FEM and the quasi-Hertz approach have been used to model the results of the interaction between wheel and rail surfaces on how contact stresses and zones are distributed [6]. Scientists have attempted to resolve the Hertzian contact for the minute radius of curvature using analytical as well as FE modeling to evaluate the adjustment of the highest stress of contact in the rail concerning the change

in rail radii of curvature [7]. Wheel and rail contacting profiles deteriorate over time due to wear. Abrasion, also and surface plastic distortion are both included. The change in the geometry profile affects the stress distribution over the rail. To calculate the change in the rail profile a 3D digital model is used. Thanks to various recent technical advancements, 3D digital models of components have become more useful for tracking the progression of wear in mechanical and biological applications[8][9], [10]. As the government has brought new locomotives to work with the damaged rails, we need to find out the effect of the worn rails on the contact stresses with standard locomotive wheels. If the new locomotives are designed to work with standard tracks, they should be able to move more efficiently and safely on standard rails than worn ones. The study takes a thorough approach to the subject, starting with a theoretically grounded analytical examination of the contact involving the wheel and the rail using Hertz's hypothesis of contact. Standard UIC54, real worn UIC54 rail profiles, and a standard wheel are used to evaluate the effect of the ENR worn rails on stress analysis with new locomotives.

## 2 METHODOLOGY

Using finite element software (ANSYS), the study was divided into two main parts. The following methodology was used to meet the aim of the research:

- By first checking earlier mathematical models, and FE procedures, and validating results by simulating the interaction between wheel and rail using finite element software (ANSYS).
- After that, create a simulation model using ANSYS to show the effects of worn rails on the change of stress distribution due to the interaction between wheel and rails for ENR locomotives with the help of a case study at Port-Said railway tracks.

### 2.1 Wheel-rail Contact Model Using Mathematics

Heinrich Hertz, a German scientist who developed the Hertzian Contact Hypothesis in the year 1882, gave it that name. It includes hypotheses that lay the theoretical groundwork for the wheel-rail steady-state contact under rolling situations. Calculations of contact stresses and contact geometry are done using the theory of elastic deformation. The contact region between two elastic nonconforming objects adopts an elliptical shape with a half-major axis (a) along with a half-minor axis (b) as determined by the researchers. [11]. The distribution of the amount of pressure from contact in this elliptical area in Figure (1) represents a semi-ellipsoid, expressed as:

$$p = p_o \sqrt{\left(1 - \frac{x^2}{a^2} - \frac{y^2}{b^2}\right)} \quad (1)$$

$$a = m \left[ \frac{3\pi P(K_1 + K_2)}{4(A+B)} \right]^{1/3} \quad (2)$$

$$b = n \left[ \frac{3\pi P(K_1 + K_2)}{4(A+B)} \right]^{1/3} \quad (3)$$

Where  $K_1$  and  $K_2$  are constants that depend on the material properties of railway wheel and rail respectively.

$$k_1 = \frac{1-\nu_1^2}{\pi E_1} \quad (4)$$

$$k_2 = \frac{1-\nu_2^2}{\pi E_2} \quad (5)$$

Where  $\nu_1$  and  $E_1$  are Poisson's ratio and young's modulus of the railway wheel material and  $\nu_2$ , and  $E_2$  are Poisson's ratio and young's modulus of railway rail material.

Understanding some of the mathematical constants used in the formula above is necessary for calculating the contact areas.

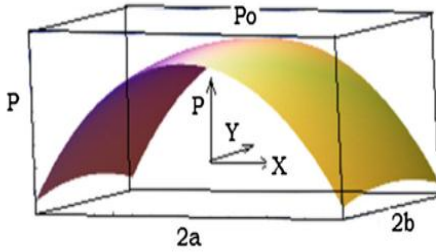


Figure 1: Pressure distribution across the elliptic area

The next curved ratios are connected in terms of a wheel-rail combination:

$$A + B = \frac{1}{2} \left( \frac{1}{R_{11}} + \frac{1}{R_{12}} + \frac{1}{R_{22}} + \frac{1}{R_{21}} \right) \quad (6)$$

$$B - A = \frac{1}{2} \left[ \left( \frac{1}{R_{11}} - \frac{1}{R_{12}} \right)^2 + \left( \frac{1}{R_{22}} - \frac{1}{R_{21}} \right)^2 + 2 \left( \frac{1}{R_{11}} - \frac{1}{R_{12}} \right) \left( \frac{1}{R_{22}} - \frac{1}{R_{21}} \right) \cos 2\psi \right]^{1/2} \quad (7)$$

where A and B are positive constants. The four most important relative curvature radii are R11, R12, R21, and R22.

Figure (2) provides a visual representation of this idea. R21 is the runway's radius, which in this case is infinite, and R22 is the rail's curvature in the cross-sectional plane. R11 is the curvature of the rolling radius of a wheel. R12 is the wheel profile radius, which for a conical wheel goes to infinity. The factors "m" and "n" relate the mathematical parameter A/B with the ellipticity parameter a/b. The notation reads  $\cos\psi = (B-A)/(A+B)$ . The amounts of m and n for different values are calculated using the tables.[12]. Regression is used to obtain the intermediate values utilizing the most effective curve-fitting method, as illustrated in Figures (3), and (4).

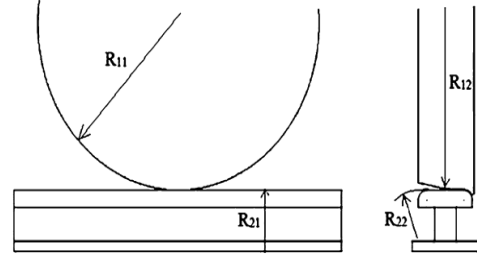


Figure 2: Wheel rail arrangement illustrating several major curvatures.

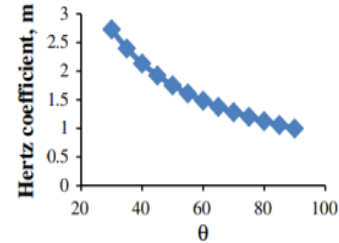


Figure 3: Hertz coefficient, "m," and "  $\theta$  " on a graph.

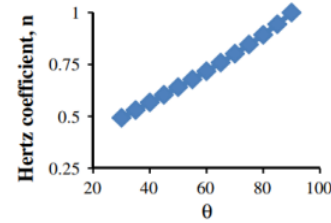


Figure 4: Hertz coefficient, "n," and "  $\theta$  " on a graph.

## 2.2 Contacting profiles

In Egypt, the UIC54 rail is the most often used. Its transverse head profile is shown in Figure (5) as a collection of circular curves with varying radii of 13, 80, and 300 mm. The components of the profile on the 13, 80, and 300 mm radii are, respectively, the rail gauge corner, rail shoulder, and rail crown. The transverse movement of the wheel may cause first contact to occur on each section of the profile. In this paper contact nearby of radius 300 is taken into account with the wheel tread. The profile radii can change over time as a result of surface wear and plastic deformation. To investigate the influence of the rail profile's change on contact stresses, pressure, and fatigue lifetime for both static and dynamic conditions a standard ENR UIC54, a real worn ENR UIC54 rail profile from ENR, and a wheel profile as per Egyptian standards are used as shown in figure (6).





across the points at the wheel's carrying location where the axle is placed. Horizontal external forces were ignored aside from actual contact conditions because of the cant angle. using the identical material data, elasticity modulus,  $E= 207\text{GPa}$  and  $205\text{GPa}$  for rail and wheel respectively, and Poisson's ratio,  $\nu = 0.3$ . It is assumed that the rail and wheel are linearly elastic.

### 2.4 Analysis of Fatigue

Based on the results of the FE study, this part gives the estimate for fatigue life. Three phases are often used to describe the life of a fatigue crack: crack start and development. These three phases include Phase 1, which is surface shearing stress-driven beginning, Phase 2, which is transitory cracking behavior, and Phase 3, which is the phase after tension and fracture-driven propagation of cracks. Fracture first manifests at moving contact points as a result of accumulated deformation caused by shear from multiple rolling-sliding contact stresses [15]. When phase 1 is finished, initiation may be seen to have happened. Jiang suggested using a straightforward damage factor for a fatigue lifetime calculation [16].

**Table (1) The mechanical characteristics of the rail and wheel material**

E Rail (GPa)	E Wheel (GPa)	$\nu$
207	205	0.3

### 2.5 Case Study and Measuring Instrument

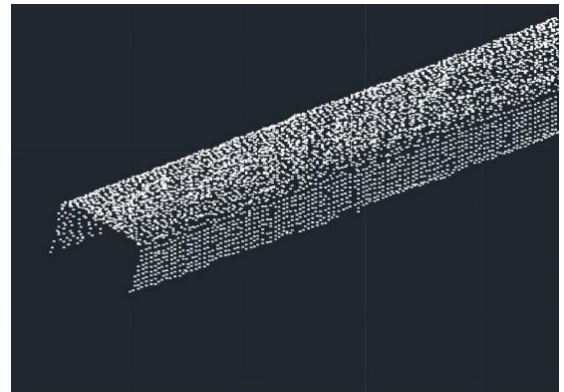
A 3D laser scanner is used to evaluate wear for the rail profile at the port-said railway station as shown in figure (9). The Leica Scan Station P40 laser scanner offers the highest versatility including long range, speed (up to 1 million points per second), and accuracy (3D positional accuracy of 3mm at 50m and 6mm at 100m). The instrument enables 3D scanned data to be used directly in any CAD software. The worn rail portion in Figure (10) was scanned and carried out in CAD3D-environment figures (11), (12). A cross-section is taken in the rail data points and carried out in Solid work to be extruded for the study as shown in Figure (13).



**Figure 9: P40 3D Laser Scanner**



**Figure 10: worn rail**



**Figure 11: Isometric of the worn railhead**



**Figure 12: Cross-sectional of the worn railhead**

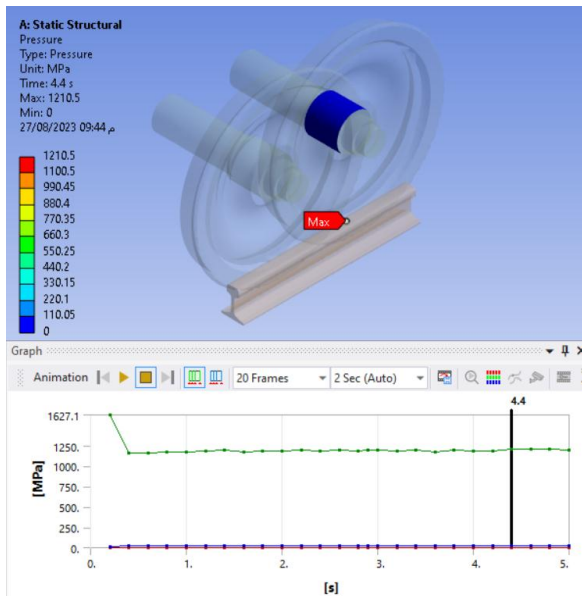


**Figure 13: Solid work for a cross-sectional of the worn railhead**

After that, the model geometry was loaded into FE ANSYS. The scanning phase targets only the rail head. This research will analyze the assembly when the wheel is positioned on the rail just over the sleeper and the dynamic motion analysis of the wheel on the rail with a velocity of 80 km/h.

### 3 RESULTS AND DISCUSSION

For the validation of standard UIC54, On the rail surface's top, the contact pattern is shown. Hertzian analytical calculation result for the contact pressure distribution is 1236.6 MPa and as shown in figure (14) the FE result from the software ANSYS is 1210.5 MPa. The FEM result is close to the analytical answer. These results are more realistic and accurate when compared to the calculations obtained in previous studies[17][13].

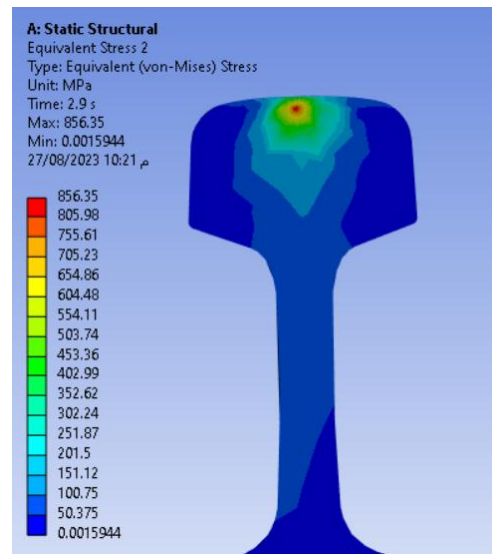


**Figure 14: Contact pressure distribution in the contact region**

Analysis of both static and dynamic loadings was done. The rail's and wheel's corresponding Von-Mises stress distributions were found. The loading evaluations were done for the wheel when it was just above the sleeper on the rail. The worn rail as well as the standard

rail have been examined. As can be seen in Figure (15) the stress on the standard rail is 856.35 MPa. Stress is higher than yield stress. The portions above the yield point suffered permanent deformation, and the head of the rail experienced the start of corrugation development caused by static stress. the contact area's stress distribution is not uniform. Red areas of the contact area cause the most stress while lesser stress is shown elsewhere. This is a consequence of the different contact profiles of the rail and wheel. Compared to the stresses from earlier research, these results are more accurate and realistic[13][18]. the Von-Mises stress of the worn rail is 523.46 MPa as shown in figure (16). The worn profile was discovered to have lower contact stresses than the standard which matches previous work[19]. Contact stresses for the worn rail profile are up to 40% lower than those for an unused ENR rail profile. Compared to the standard rail, the worn rail has a larger radius of curvature. This explains the findings since lower stresses are created with larger contact areas when the same load is applied. In general, terms, when a load causes two surfaces with differing

curvature radii to come into touch, the surface with the smaller radius of curvature tends to experience higher contact stress in the immediate region of contact. This is because a smaller radius of curvature leads to a smaller contact area, which results in higher pressure (force per unit area), leading to higher stress. As shown in Figures (17), and (18), the contact area for the worn rail is much greater than the contact area of the standard rail.



**Figure 15: Von-mises stress distribution for standard rail**

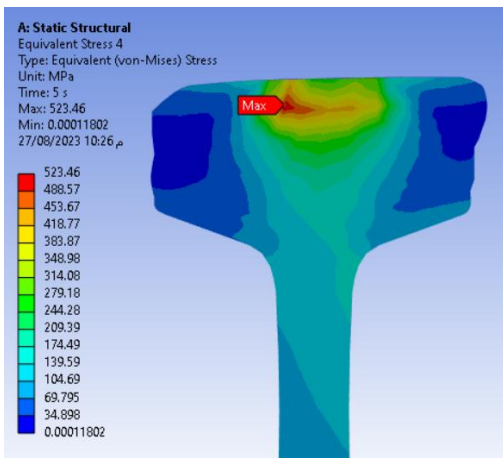


Figure 16: Von-mises stress distribution for worn rail

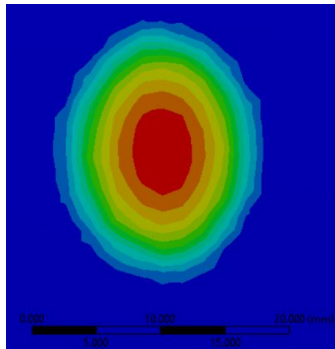


Figure 17: Contact area for standard rail

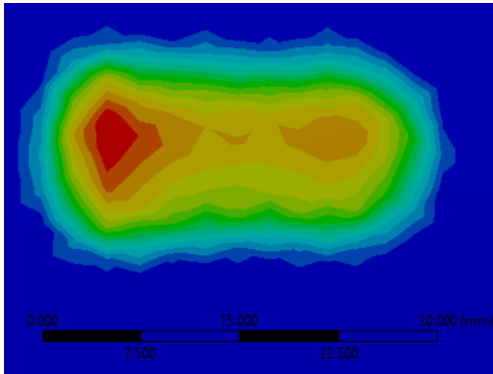


Figure 18: Contact area for worn rail

The most critical location for the beginning of a fatigue fracture is thought to be the highest von Mises stress point. Using FE, for standard and deteriorated rail profiles, damage caused by fatigue and the total number of failure cycles are calculated. The results are regardless of the cracks propagated on the worn rail or any other defects. The FE deals with the rail changes from a profile point of view. Figures (19), (20), (21), and (22) demonstrate that a number reduction in life cycles is found and that the fatigue damage rises as the contact stresses decrease as predicted. Smaller radii of curvature can lead to stress concentration points, where the stress is significantly amplified compared to the average stress in the structure. These stress concentration points are more likely to initiate cracks and other forms of damage, which

can eventually lead to fatigue failure. Larger radii of curvature help distribute stress more evenly and reduce the likelihood of stress concentration.

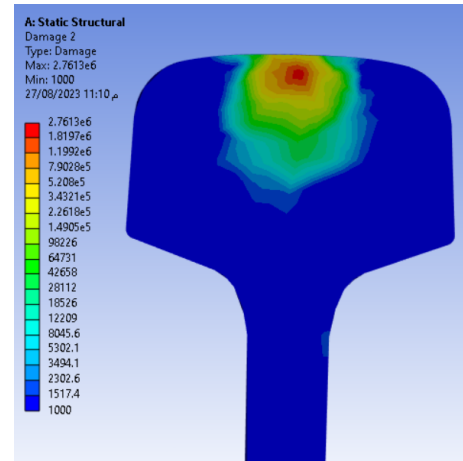


Figure 19: Fatigue damage for standard rail

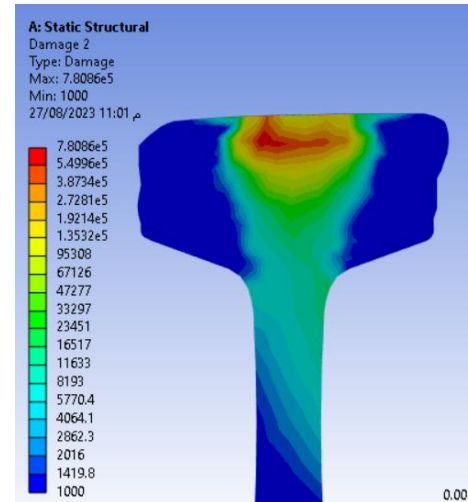


Figure 20: Fatigue damage from worn rail

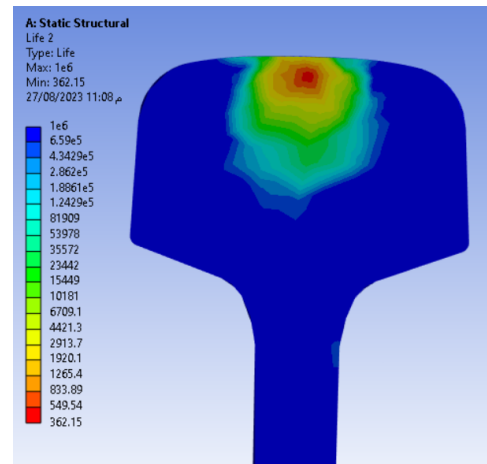


Figure 21: Fatigue life for standard rail

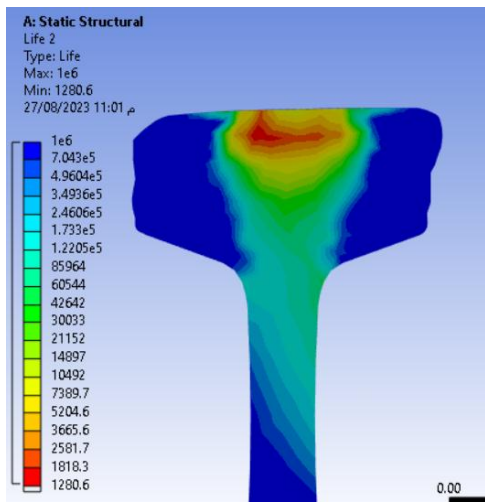


Figure 22: Fatigue life for worn rail

On account of the dynamic relation between the rail and the wheel, analysis was done with the assumption that the wheel velocity was 80 km/h. As shown in figure (23) Von-Mises stress value exceeds the yield stress for both standard and worn rail respectively 2111 MPa and 1114 MPa. The standard profile's contact stresses were found to be higher than those of the worn profile because of the variation of the profile curvature as explained before. The dynamic stress variation for the standard rail is larger than the worn one. the lower stress range means the initiation and propagation of cracks occur at a slower pace. This can result in a longer lifespan for the material before failure.

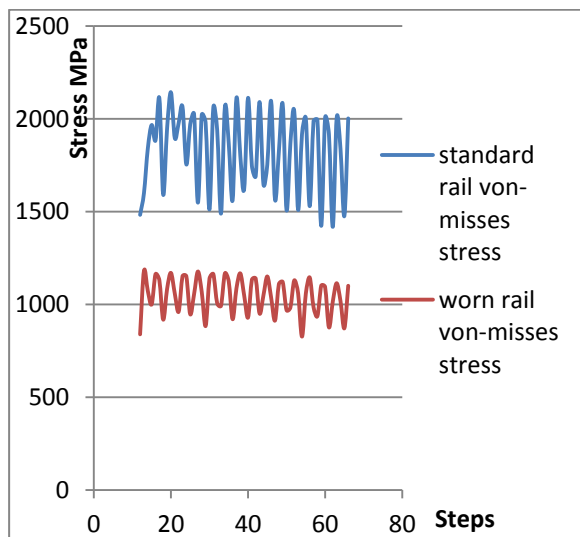


Figure 23: Von Mises stresses for dynamic load for standard and worn rail

Conicity which is the outcome of the mutual fit of the rail and wheel, is known as the “equivalent cone angle” of a specific track-wheelset combination. When a wheelset moves in one direction or the other, it may automatically guide itself back to a path halfway between the rails. High conicity can cause dynamic instability,

sometimes known as "hunting," which significantly affects the ride and can harm the track. The worn rail case improves the fit between the wheel and rail, reducing contact stresses. Therefore, decreasing contact stresses will be followed by a rise in conicity which leads to a stress increase at the edges where the wheels make more contact and instability in the track moving. [19]

#### Credit Authorship Contribution Statement:

**Ismail Mohsen:** Methodology, Writing Original Draft, Software.

**Ashraf El-Sabbagh:** Conceptualization, Review and Editing, Supervision.

**Ahmed Adel Turk:** Supervision, Review, and Editing.

#### Declaration of Competing Interest

The writers claim to not know about competing financial interests or personal relationships that could have appeared to influence them.

## 4 CONCLUSIONS

In this research, the dynamic and static contact studies of a standard ENR UIC54, a real worn ENR UIC54 rail profile, and a wheel profile as per Egyptian standards were carried out through 3D FEA. Analysis was carried out using 100kN wheel loads based on the conditions in which the wheel is on the sleeper. contact stresses, pressure, and fatigue lifetime for static and dynamic conditions are figured comparatively. A 3D laser scanner is used to evaluate wear for the rail profile at the port-said railway station so a real worn rail profile is used in this study. Using stress distribution obtained through FEM analysis, the effects of the change in Egyptian rail profiles with ENR New locomotives' wheel on the contact stress is investigated. Contact stresses for the worn rail profile are up to 40% lower than those for an unused ENR rail profile. These results happened as the worn rail has a larger contact area than the standard rail. Larger contact area gives less contact stress than smaller contact area. A wider contact area can also help distribute the wear more evenly across the surface of the rail and the wheel. This can lead to reduced wear and tear on both the rail and the wheel promoting longer service life. While worn rails might have less stress distribution due to the increased contact area at the rail head, the increased conicity can counteract this advantage by causing higher localized stresses at the edges where the wheels make more contact. New research on fracture development and spread in the rail as well as on abrasion in the rail and wheel will be performed after this study. It will investigate how conicity affects wheel deformation and wheel edge stresses.



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